

Experimental and theoretical studies of line-shape parameters to address the spectroscopic challenges of planetary atmospheres

Bastien Vispoel

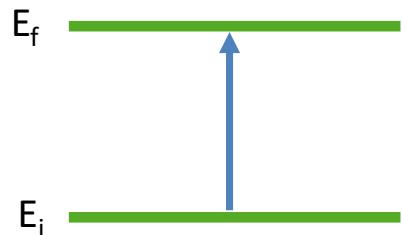
Laboratory Lasers and Spectroscopies
University of Namur, Belgium



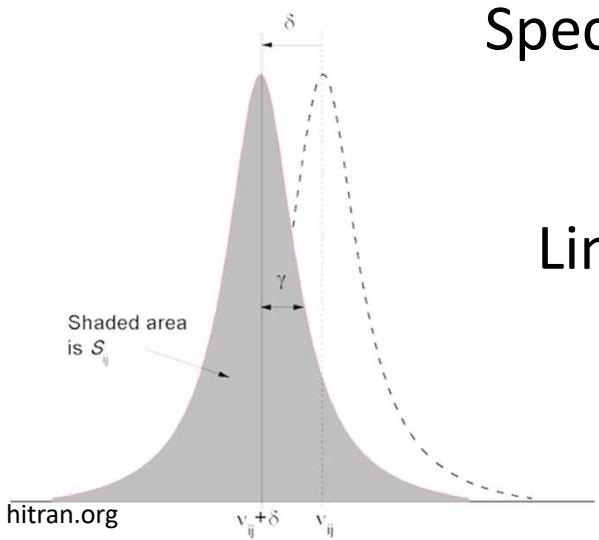
www.unamur.be



Introduction

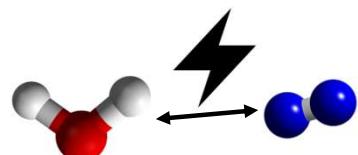


$$I = I_0 e^{-kL}$$



Spectroscopic parameters

Line-shape parameters
($\gamma_0, \delta_0, \dots$)



Atmospheric interests

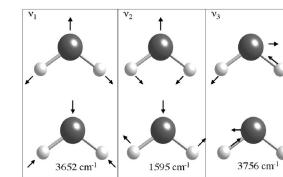


Climate changes

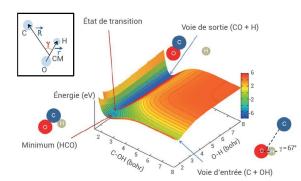


Planetary atmospheres

Fundamental interests



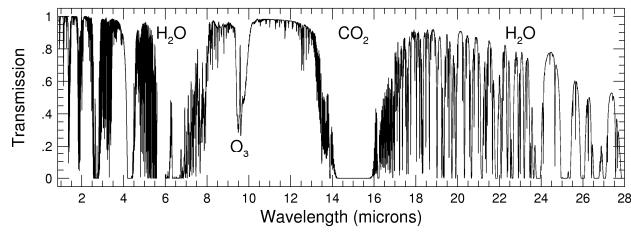
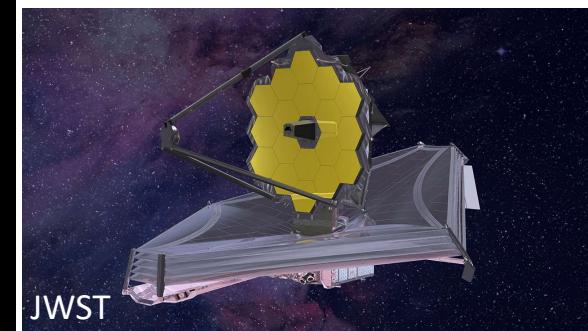
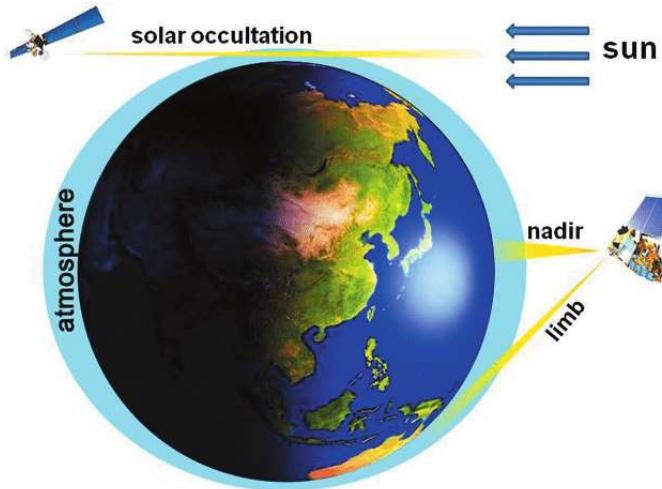
Molecular properties



Models

Introduction

Remote sensing for planetary atmospheres

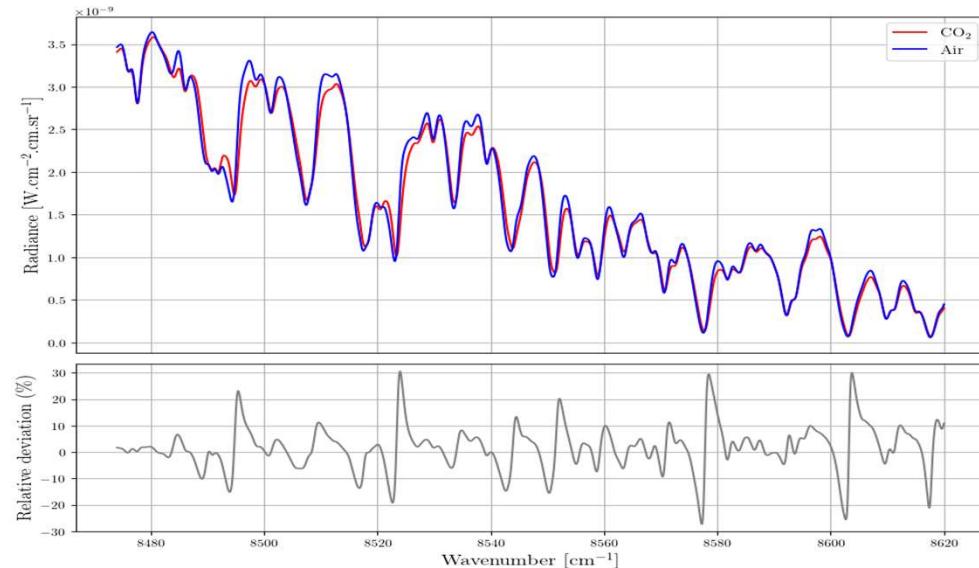
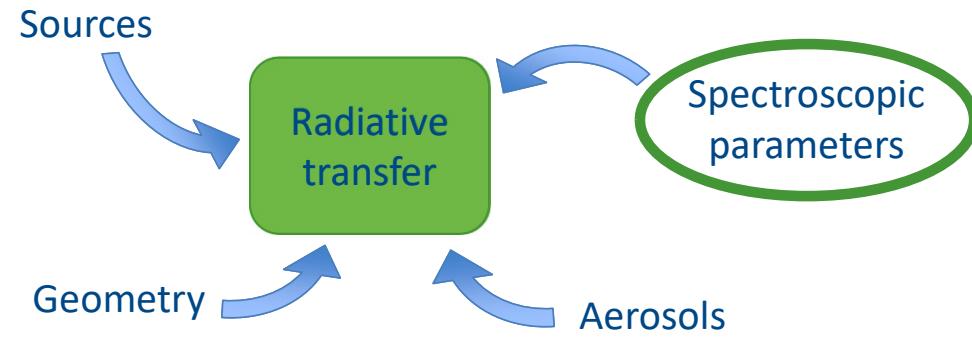


Pressure
Concentration
Temperature
...



Introduction

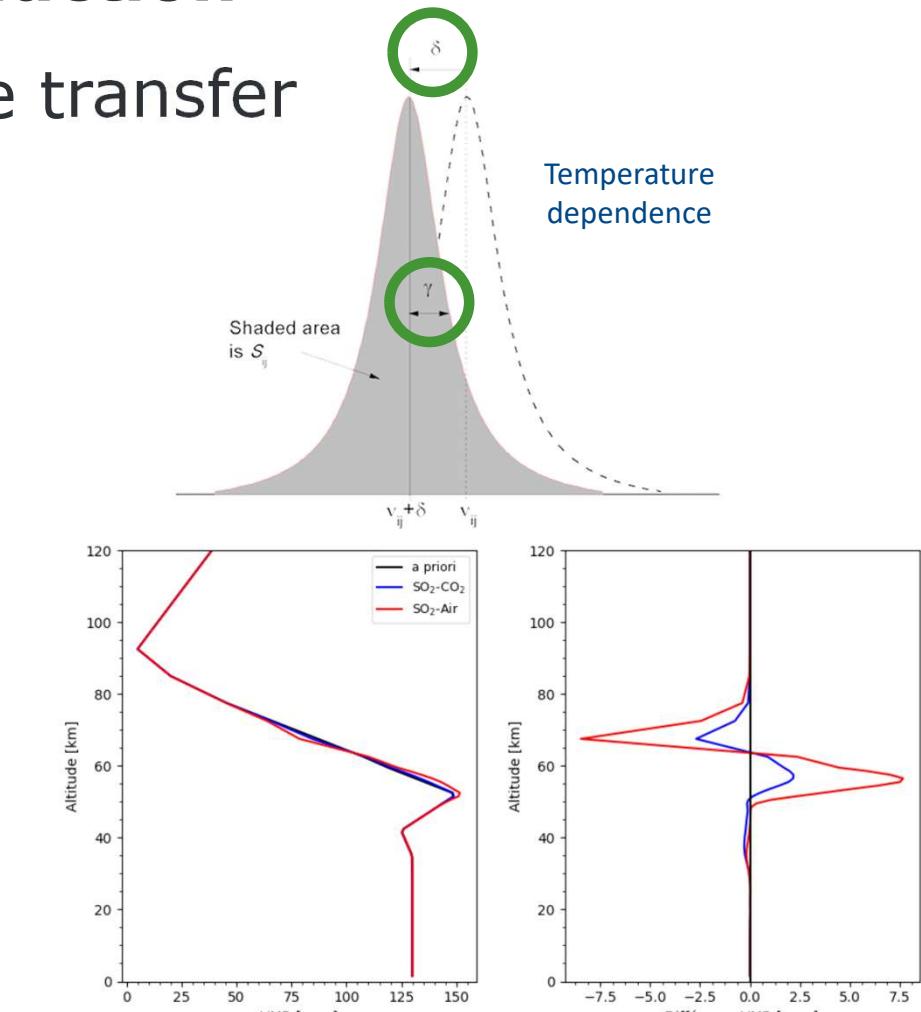
Radiative transfer



E. Ducreux, private communication

www.unamur.be

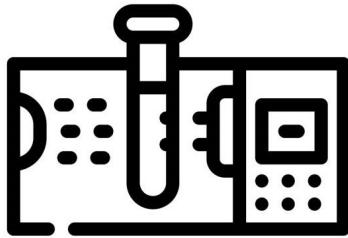
JSM2025 – Grenoble, 10-12 mars 2025



L. Fabris, Master thesis, University of Namur (2022)

Introduction

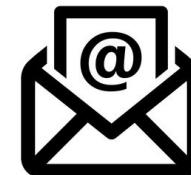
Spectroscopic challenges



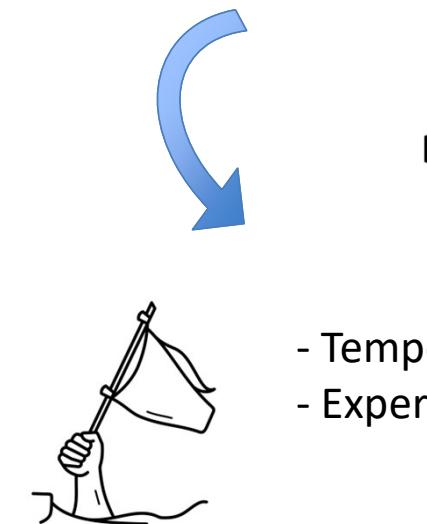
Measurement campaign: weeks, months
Spectra analysis: weeks, months
→ Dozens or hundreds of lines



Once interaction potential is known
→ Computations of thousands of lines



Ex: H_2O for VenSpec-H (4 spectral regions)
→ 5760 lines in more than 50 bands



- Temperature dependence
- Experimental difficulties

Introduction

Methodology

Measure line shape parameters



Determine intermolecular potential

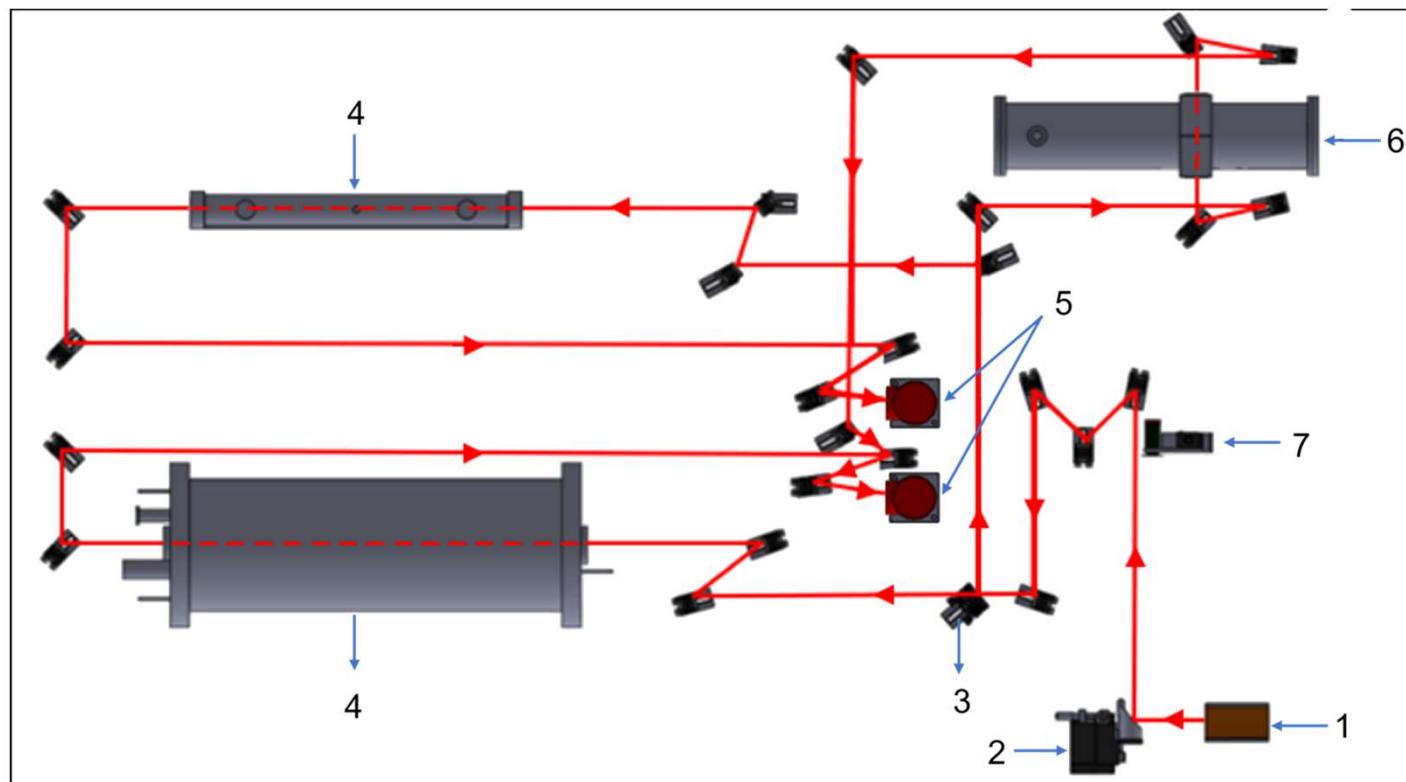


Compute line shape parameters for
many vibrational bands

$(\gamma_0, \delta_0, \text{speed and temperature dependencies})$

Laboratory measurements

QCL spectrometer



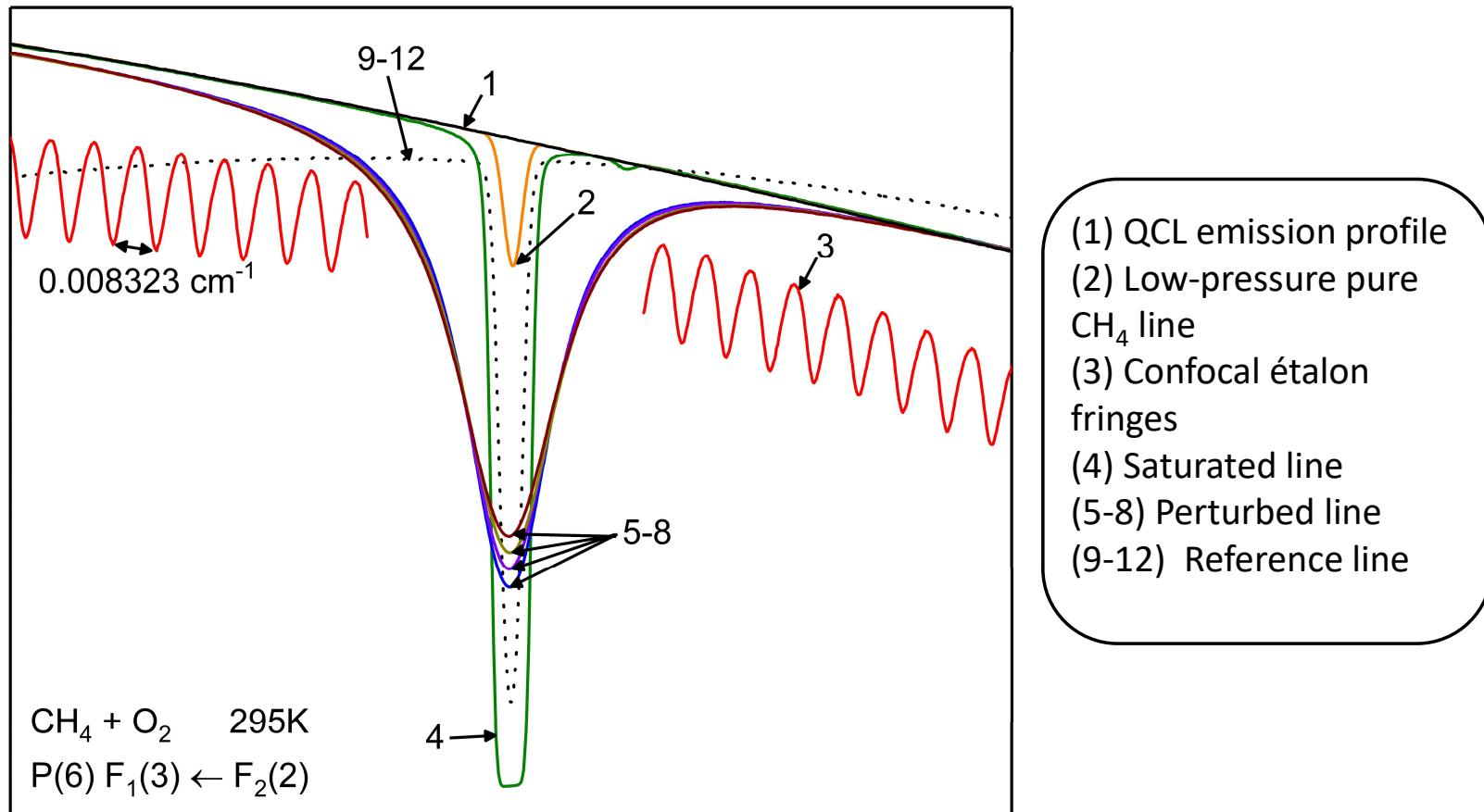
1. Quantum Cascade Laser
2. Parabolic mirror
3. Beam splitter
4. Absorption cells
5. Detectors
6. Confocal étalon
7. Chopper

Characteristics

- High-resolution ($5 \times 10^{-5} \text{ cm}^{-1}$)
- Excellent SNR (>2000)
- Spectral range (0.1 - 2 cm^{-1})

Laboratory measurements

QCL spectrometer

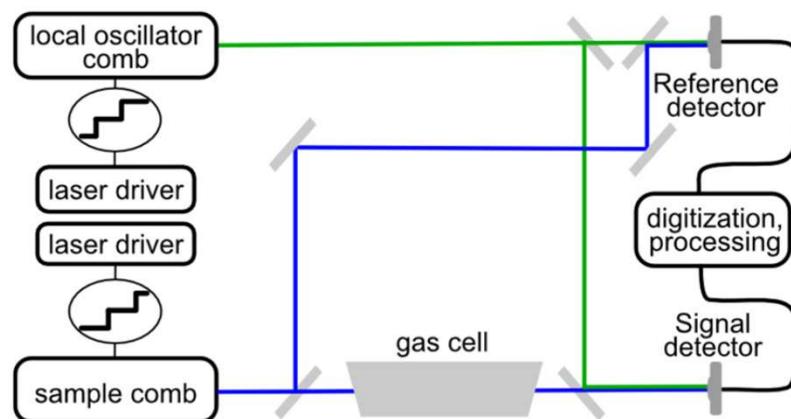


Vispoel and Lepère, HRMS 2022, Praha (Czech Republic), 2022

B. Vispoel *et al.*, JQSRT, 328, 109150 (2024)

Laboratory measurements

Dual comb spectrometer



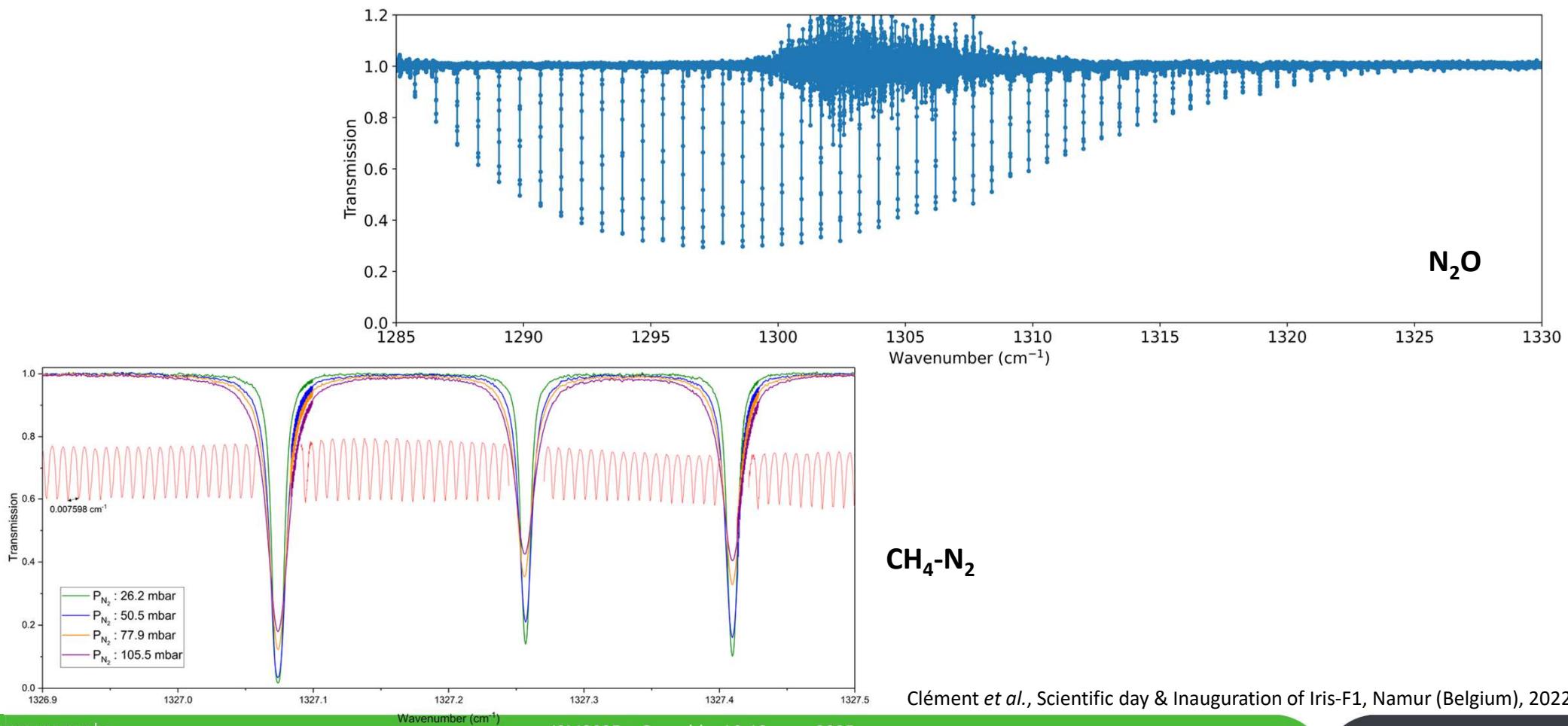
Characteristics

- High-resolution (up to $4 \times 10^{-4} \text{ cm}^{-1}$)
- Spectral range ($60\text{-}100 \text{ cm}^{-1}$)
- Acquisition time (5-7 min)
- Very good SNR (>650)

Lepère *et al.*, JQSRT, 287, 108239 (2022)
Clément *et al.*, JQSRT, under revision

Laboratory measurements

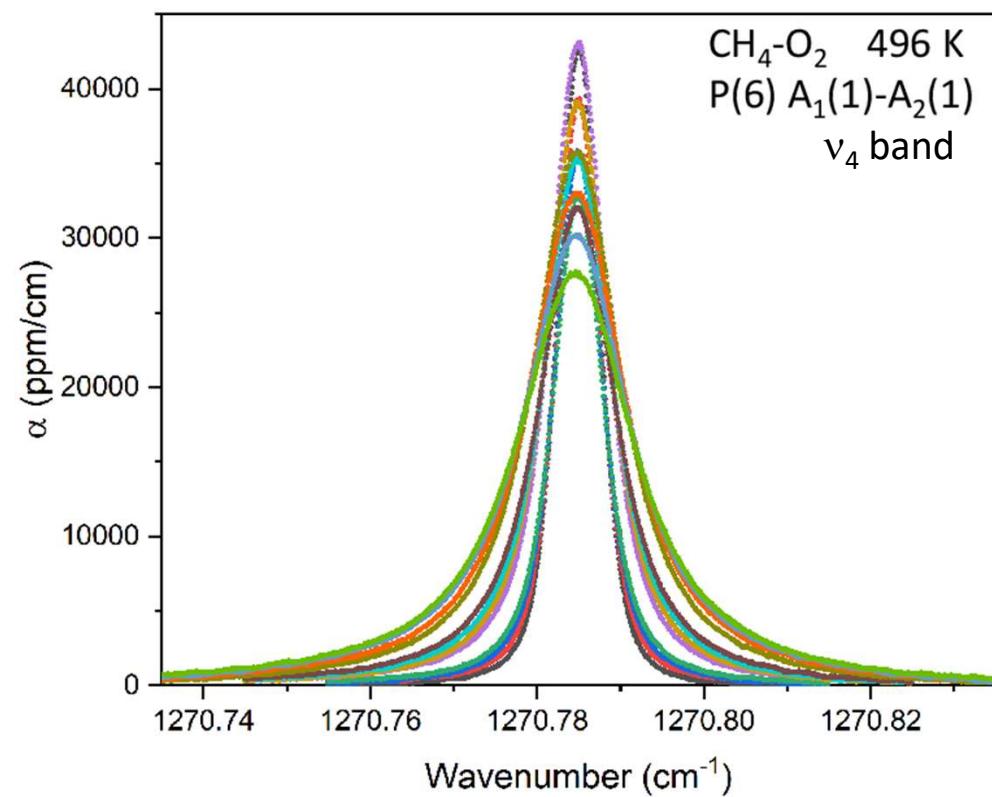
Dual comb spectrometer



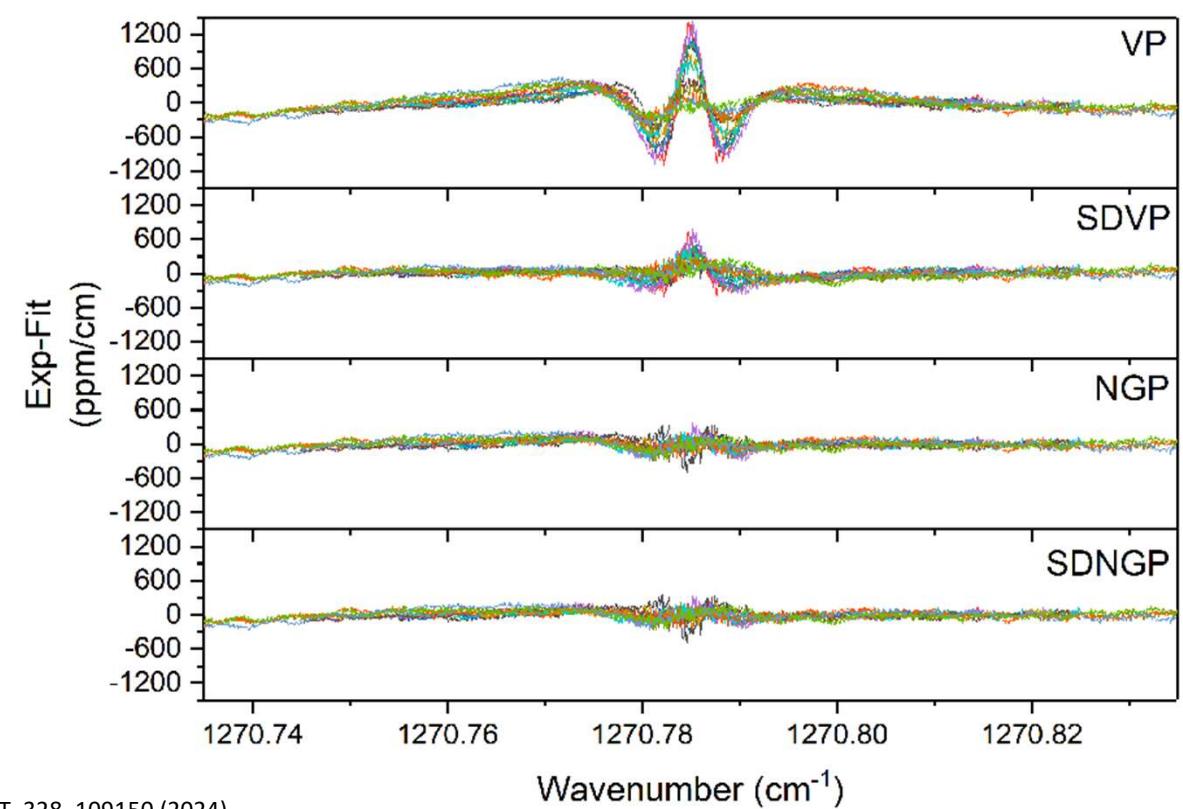
Clément *et al.*, Scientific day & Inauguration of Iris-F1, Namur (Belgium), 2022

Laboratory measurements

Experimental line profile fits

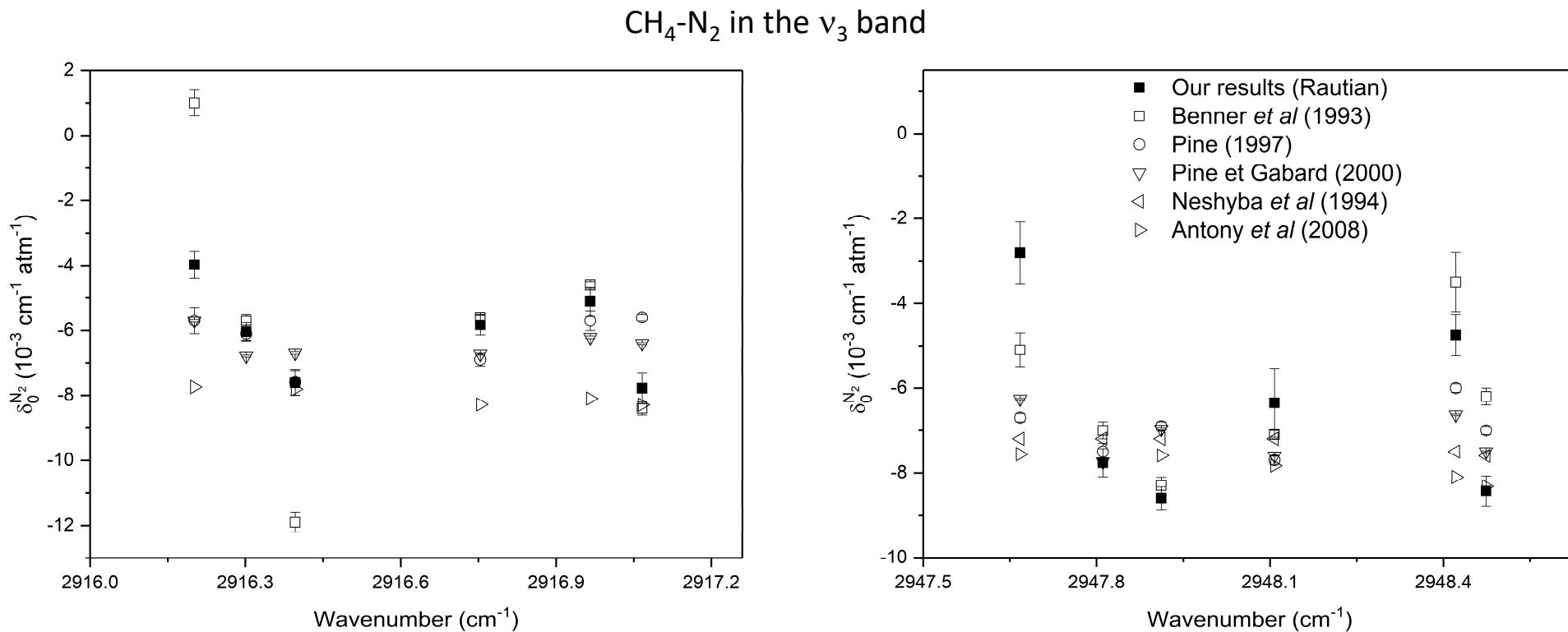


Vispoel *et al.*, JQSRT, 328, 109150 (2024)



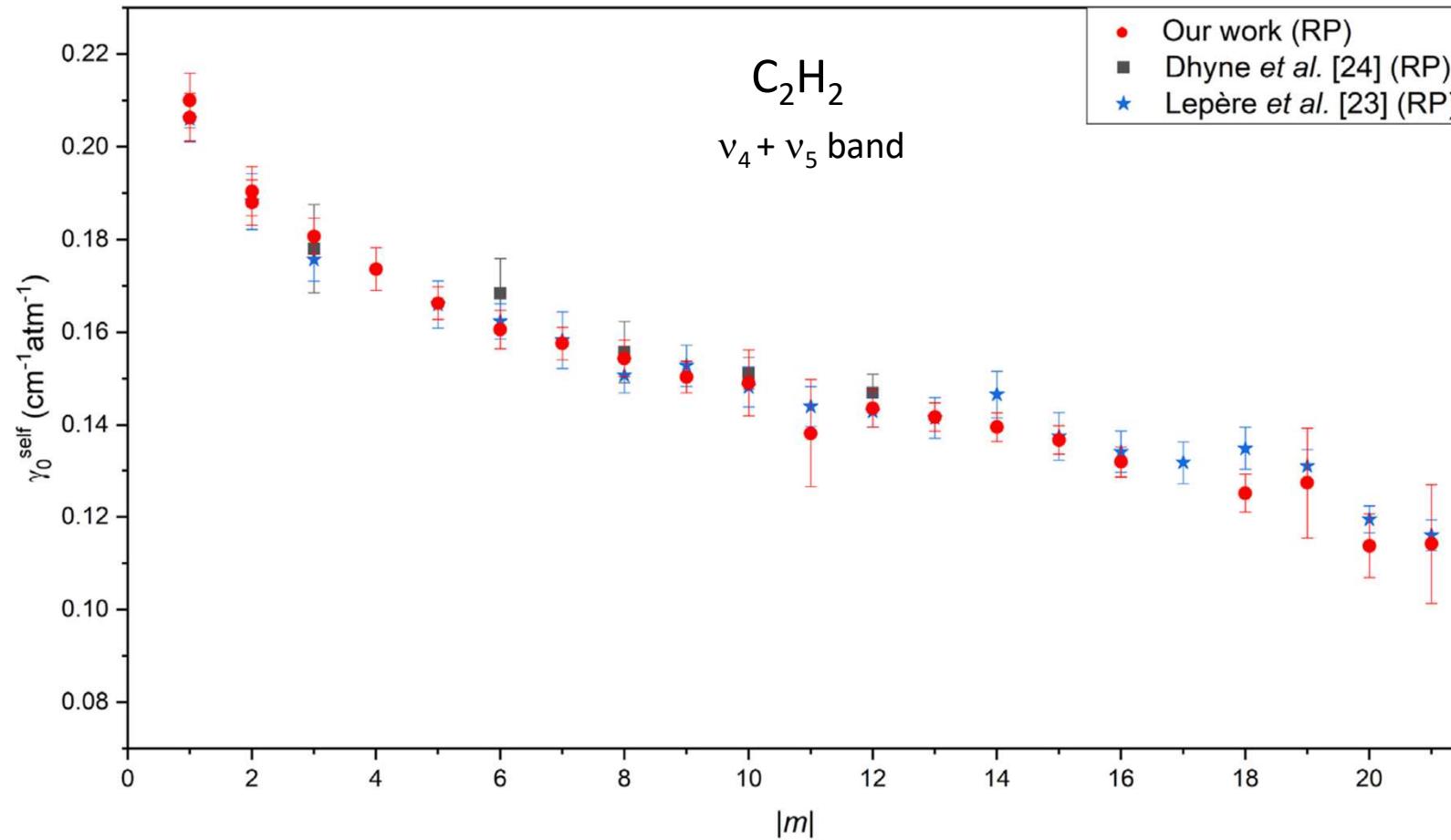
Laboratory measurements

Diode-laser experimental results



Laboratory measurements

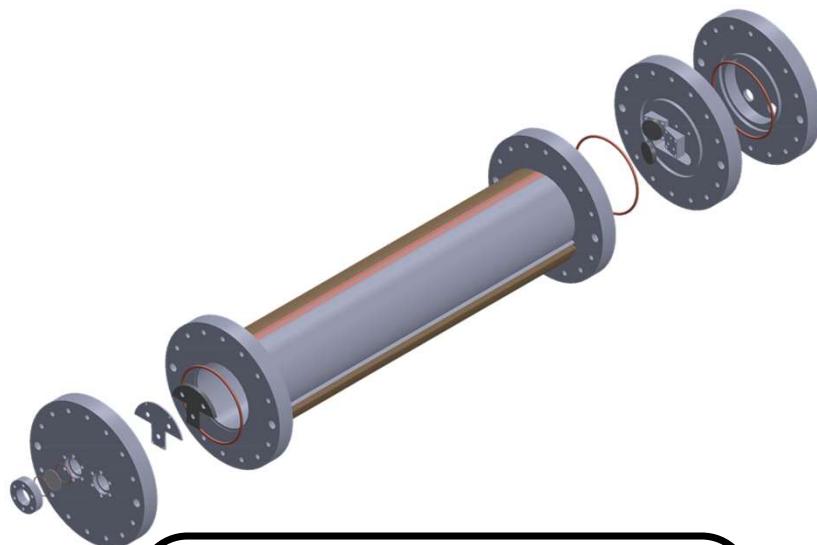
DCS experimental results



Dricot et al., JQSRT, 328, 109149 (2024)

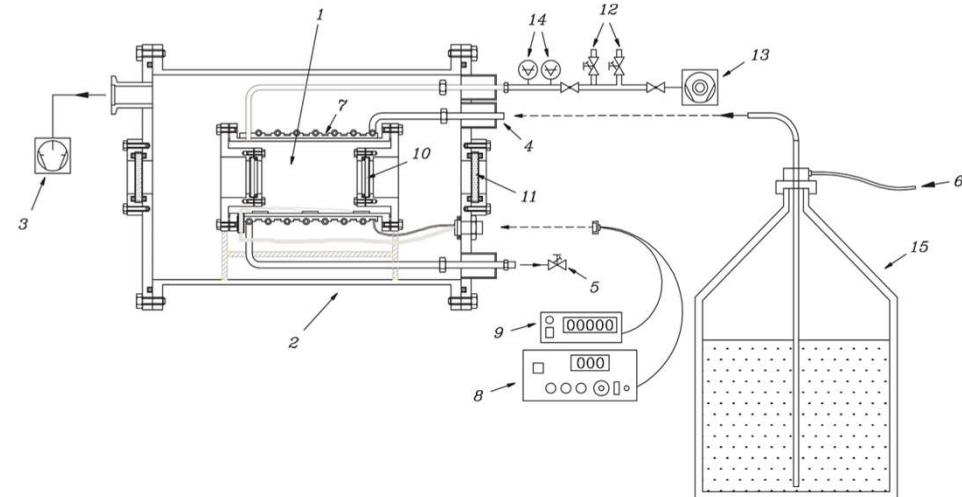
Laboratory measurements

Temperature dependence



- Temperature range: 296 - 1000 K
- Temperature stability: 1 K
- No gradient of temperature
- Single path (0.437 m) and White-type design (2 to 10 m)

Temperature range: 100 - 296 K
Temperature stability: 0.1 K
No gradient of temperature
Absorption path: 0.4043 m



Fissiaux *et al.*, JMS (2015), 317, 26
Léonis, PhD thesis (2019)

Lerot *et al.*, JMS (2003), 219, 329

Laboratory measurements

Temperature dependence

$$\gamma(T) = \gamma(T_0) \left[\frac{T_0}{T} \right]^n \quad \delta(T) = \delta(T_0) + \delta' (T - T_0)$$

Double Power Law

$$\gamma(T) = c_1 \left[\frac{T_0}{T} \right]^{n_1} + c_2 \left[\frac{T_0}{T} \right]^{n_2}$$

- Physic's based
- Large range of temperature
- Works for half-width, line shift and their speed dependence
- Allow change of sign

Gamache and Vispoel, JQSRT, 217, 440 (2018)

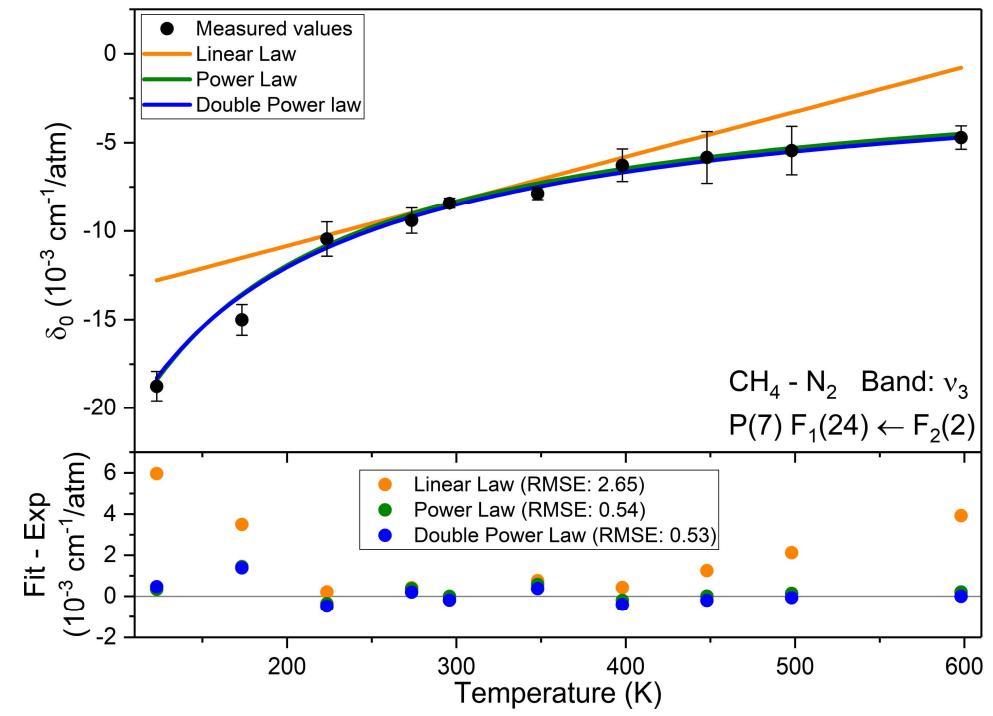
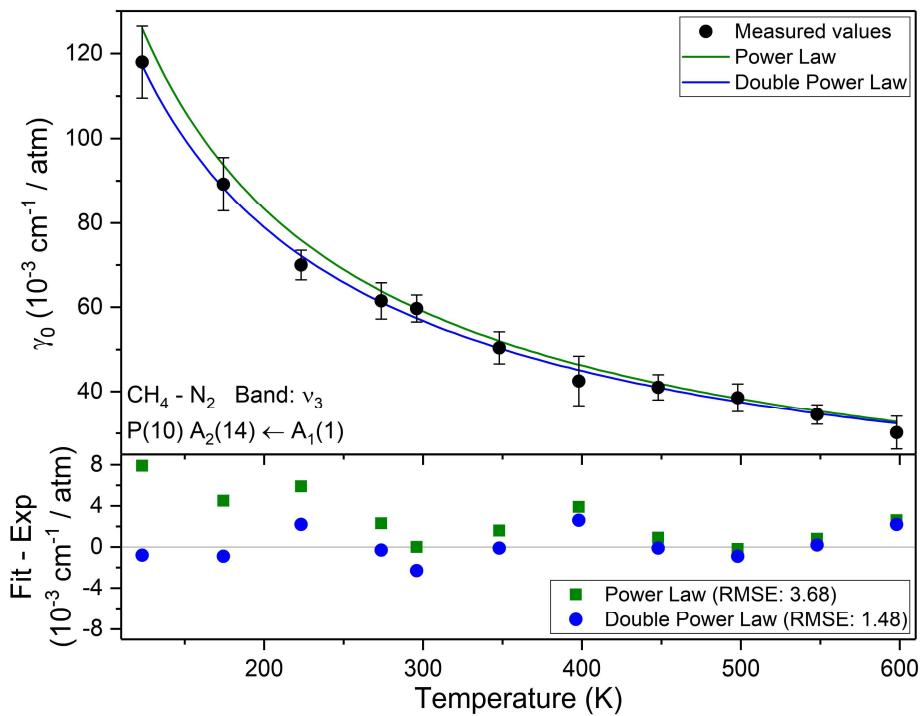
Laboratory measurements

Temperature dependence

$$\gamma(T) = \gamma(T_0) \left[\frac{T_0}{T} \right]^n$$

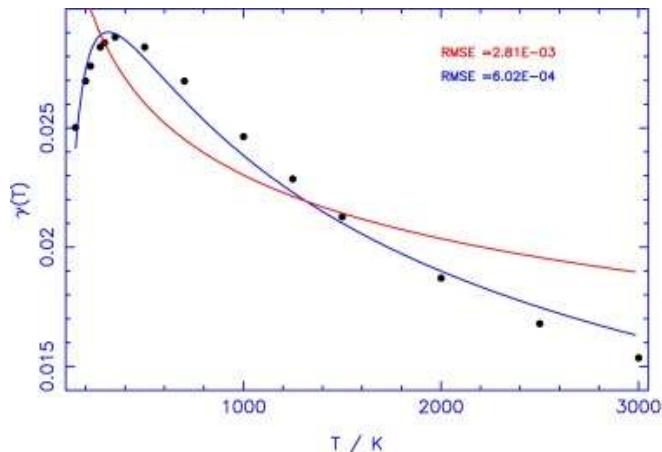
$$\gamma(T) = c_1 \left[\frac{T_0}{T} \right]^{n_1} + c_2 \left[\frac{T_0}{T} \right]^{n_2}$$

$$\delta(T) = \delta(T_0) + \delta' (T - T_0)$$

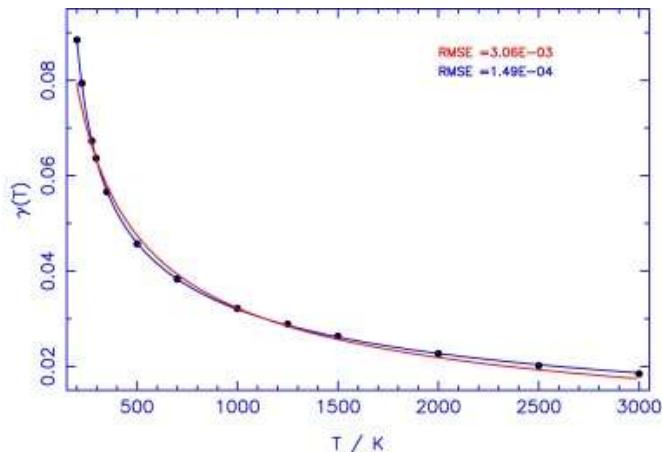


Vispoel and Lepère, Scientific day & Inauguration of Iris-F1, Namur (Belgium), 2022

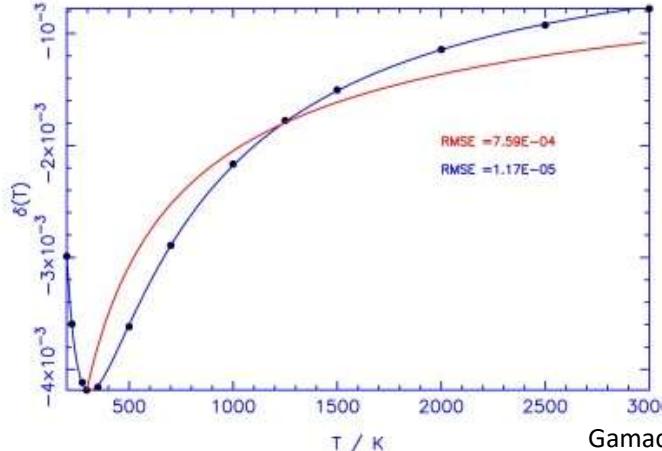
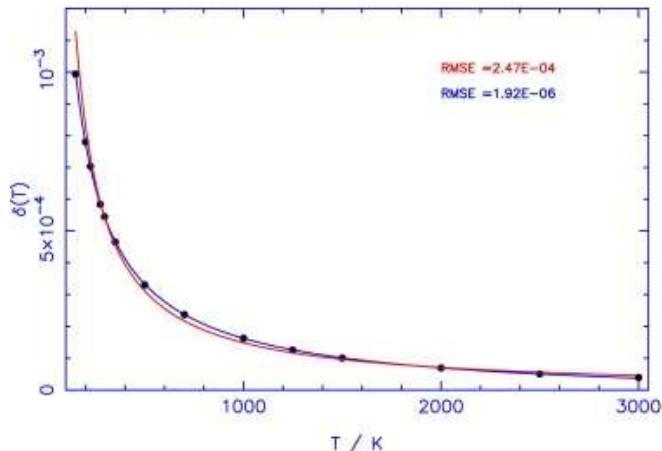
Temperature dependence of collisional line shape parameters



H₂O-N₂ 000-000 15₁₁₅ < 14₀₁₄



H₂O-H₂ 100-000 8₆₃ < 7₅₂



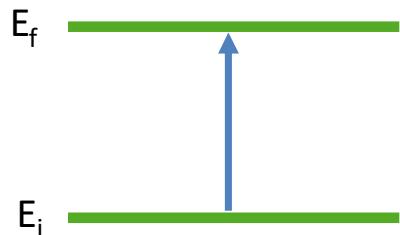
Gamache and Vispoel, JQSRT, 217, 440 (2018)

Line shape calculations

Semi-classical Complex Robert-Bonamy-Ma formalism

Why semi-classical model?

- Accuracy
- Computation resources

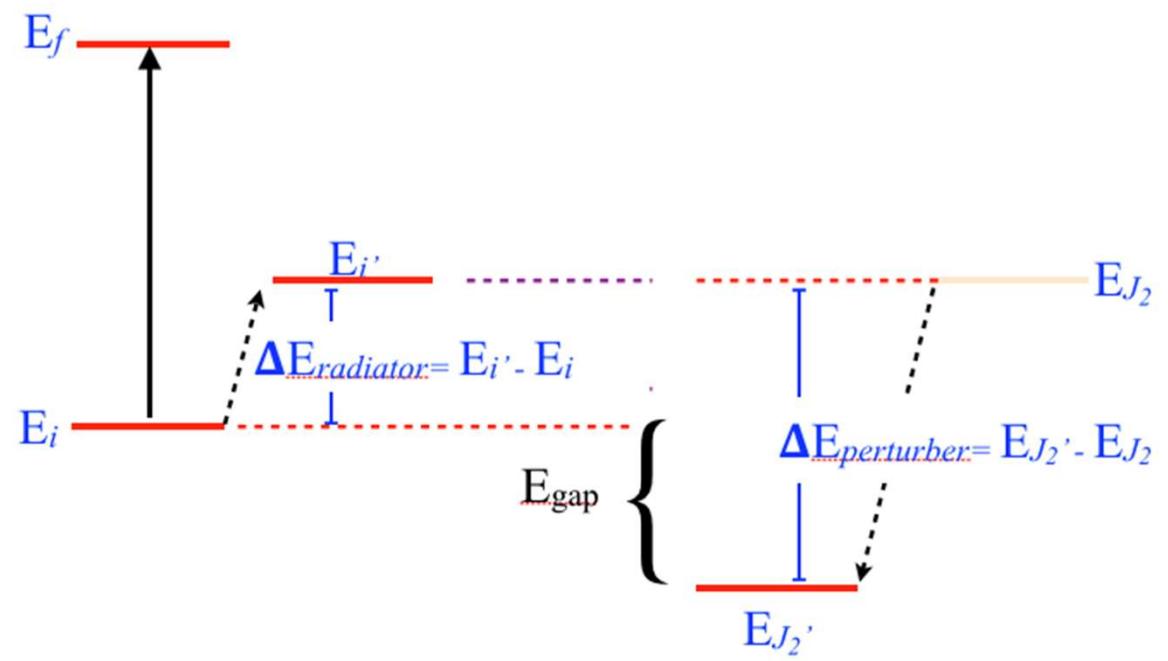
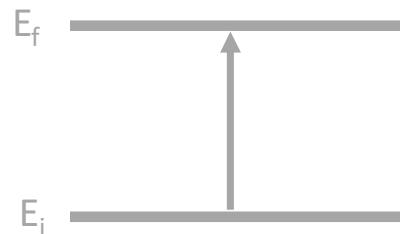


Line shape calculations

Semi-classical Complex Robert-Bonamy-Ma formalism

Why semi-classical model?

- Accuracy
- Computation resources



$$E_{gap} = \Delta E_{radiator} - \Delta E_{perturber}$$

R.R. Gamache, private communication

Line shape calculations

Semi-classical Complex Robert-Bonamy-Ma formalism

Semi-classical approach to line shape

$$(\gamma - i\delta)_{f \leftarrow i} = \frac{n_2}{2\pi c} \int_0^{+\infty} v f(v) dv \int_0^{+\infty} 2\pi b db \\ \times \left[1 - e^{-i\langle S_1 + \text{Im}\{S_2\} \rangle_{J_2}} e^{\langle \text{Re}\{S_2\} \rangle_{J_2}} \right]$$

Classical mechanics

- Trajectory
- Hamilton's equations
- Resonance function
- Explicit integration of the velocity integral

Quantum mechanics

- Internal structure: vibration & rotation
- Probability of collisionally induced transition

Line shape calculations

Intermolecular potential

- Molecular system dependent
- General combination of:
 - Electrostatic components (dipole, quadrupole, octupole, hexadecapole)
 - Atom-Atom components
 - Induction component
 - London dispersion component

$$V = \sum_{l_1 l_2 l} \sum_{\substack{n_1 m \\ m_1 m_2}} \sum_{w q} \frac{U(l_1 l_2 l, n_1 w q)}{R^{q+l_1+l_2+2w}} C(l_1 l_2 l; m_1 m_2 m) D_{m_1 n_1}^{l_1}(\Omega_1) D_{m_2 0}^{l_2}(\Omega_2) Y_{l m}(\omega)$$

4th rank ($l_{max} = 4$); 20th order ($l_1 + l_2 + 2w$)

G. G. Gray, K. E. Gubbins, Theory of Molecular Fluids, Clarendon Press (Oxford 1984)

Line shape calculations

Intermolecular potential

$$V^{at-at} = \sum_{i=1}^n \sum_{j=1}^m 4\epsilon_{ij} \left\{ \frac{\sigma_{ij}^{12}}{r_{ij}^{12}} - \frac{\sigma_{ij}^6}{r_{ij}^6} \right\}$$

n and m : number of atoms in active molecule and perturber

ϵ_{ij} and σ_{ij} : Lennard-Jones parameter for atomic pairs

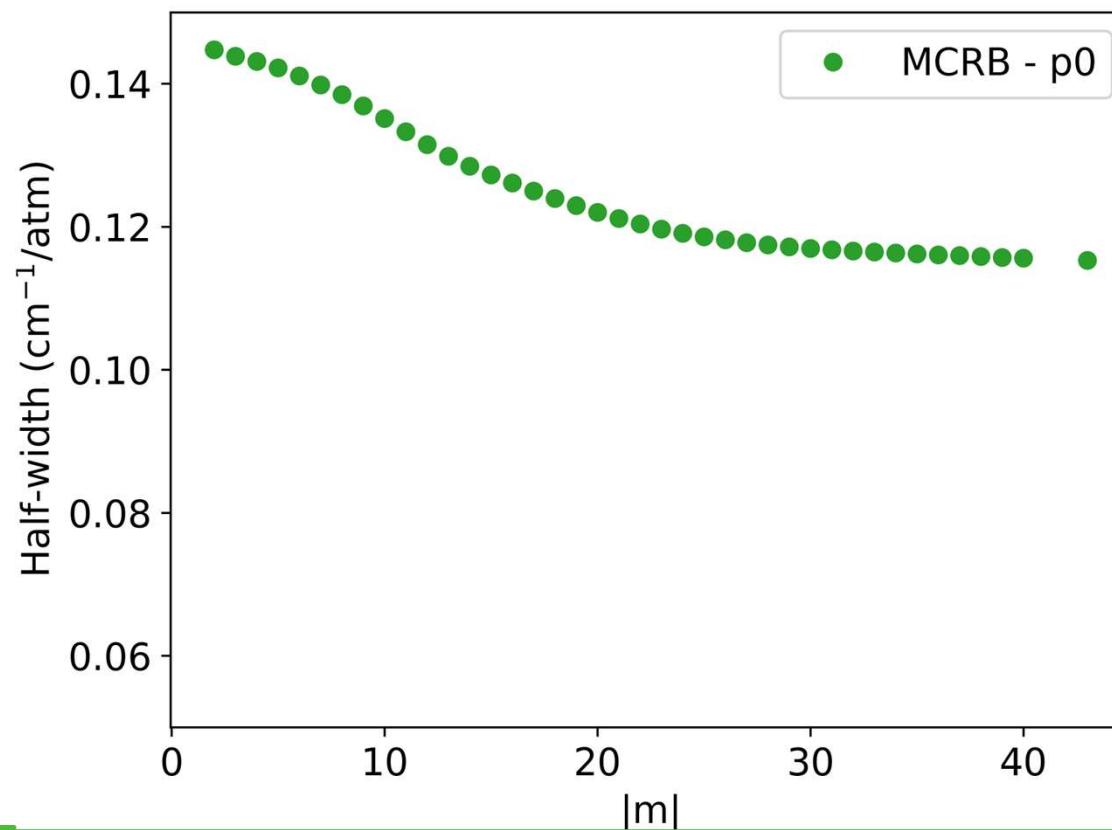
r_{ij} : atom-atom distance

- Many combination rules
- Very different results

Line shape calculations

Intermolecular potential

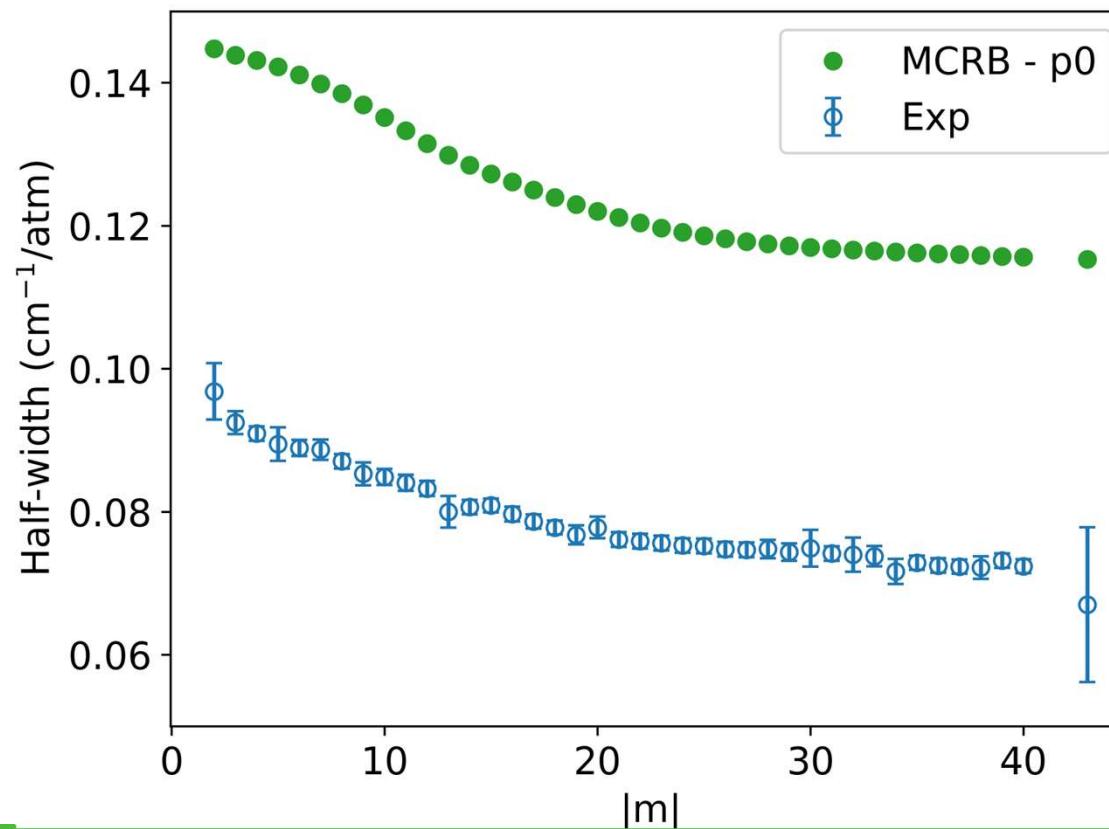
$\text{N}_2\text{O-N}_2$: ν_1 - combination rules



Line shape calculations

Intermolecular potential

$\text{N}_2\text{O-N}_2$: ν_1 - combination rules



Line shape calculations

Intermolecular potential

$$V^{at-at} = \sum_{i=1}^n \sum_{j=1}^m 4\epsilon_{ij} \left\{ \frac{\sigma_{ij}^{12}}{r_{ij}^{12}} - \frac{\sigma_{ij}^6}{r_{ij}^6} \right\}$$

n and m : number of atoms in active molecule and perturber

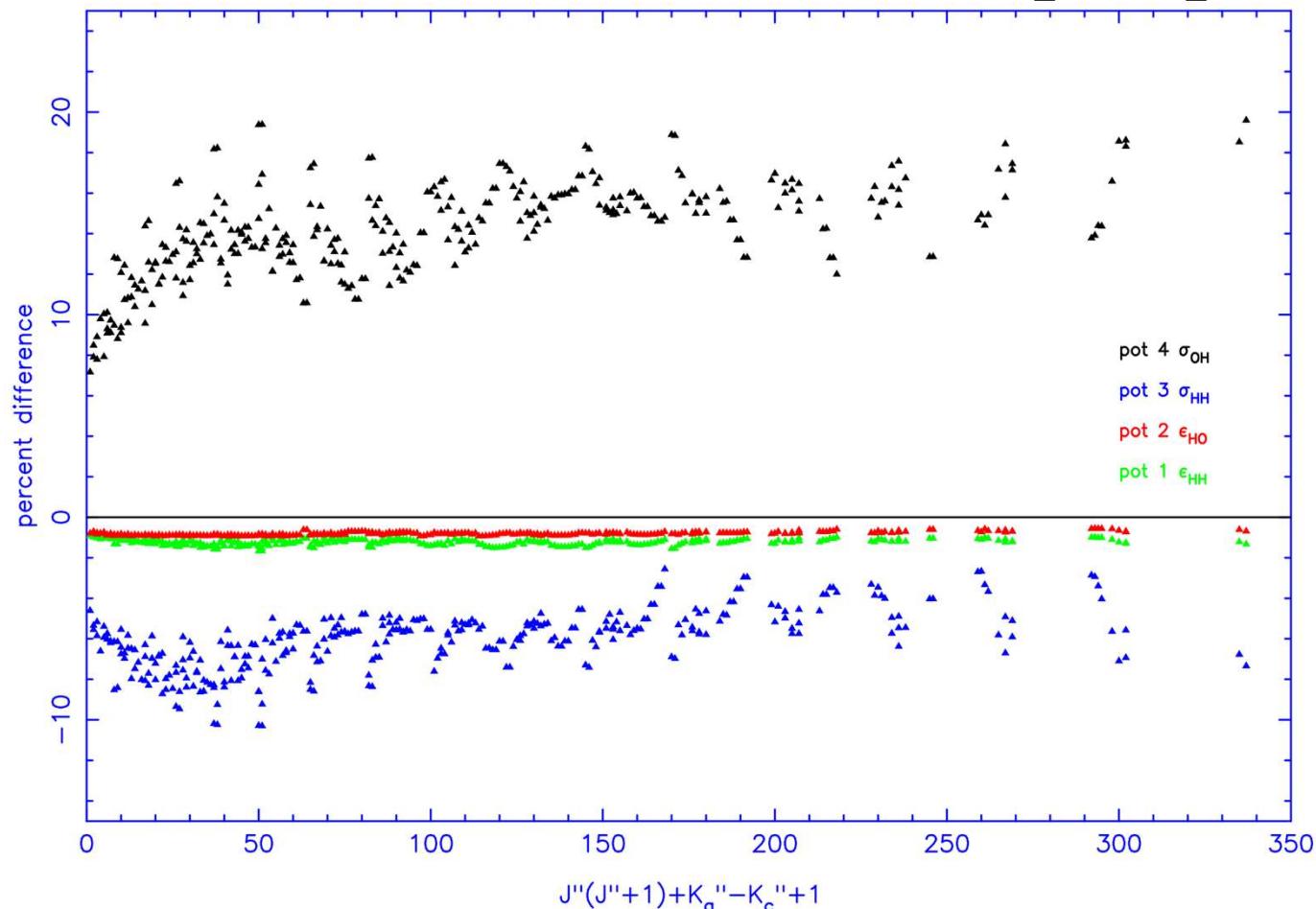
ϵ_{ij} and σ_{ij} : Lennard-Jones parameter for atomic pairs

r_{ij} : atom-atom distance

- Many combination rules
- Very different results
- Adjust at-at parameters to fit reliable experimental data

Line shape calculations

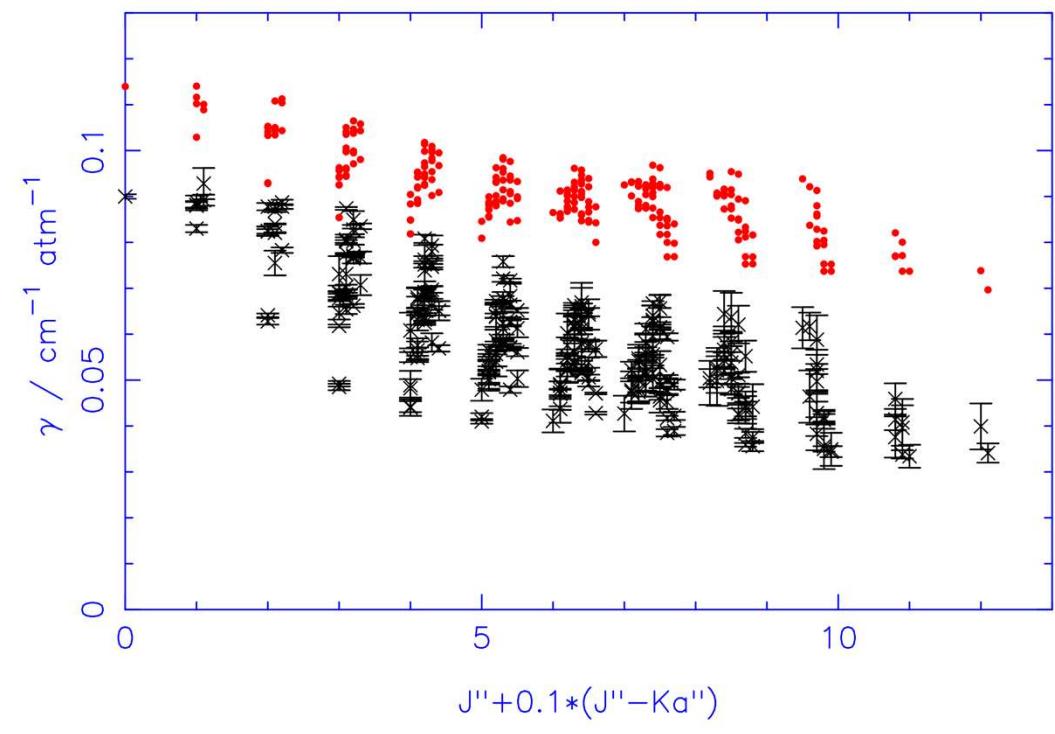
Potential determination ($\text{H}_2\text{O}-\text{H}_2$)



Renaud et al., Icarus (2018), 306, 275

Line shape calculations

Potential determination ($\text{H}_2\text{O}-\text{H}_2$)



APD: -59.12%

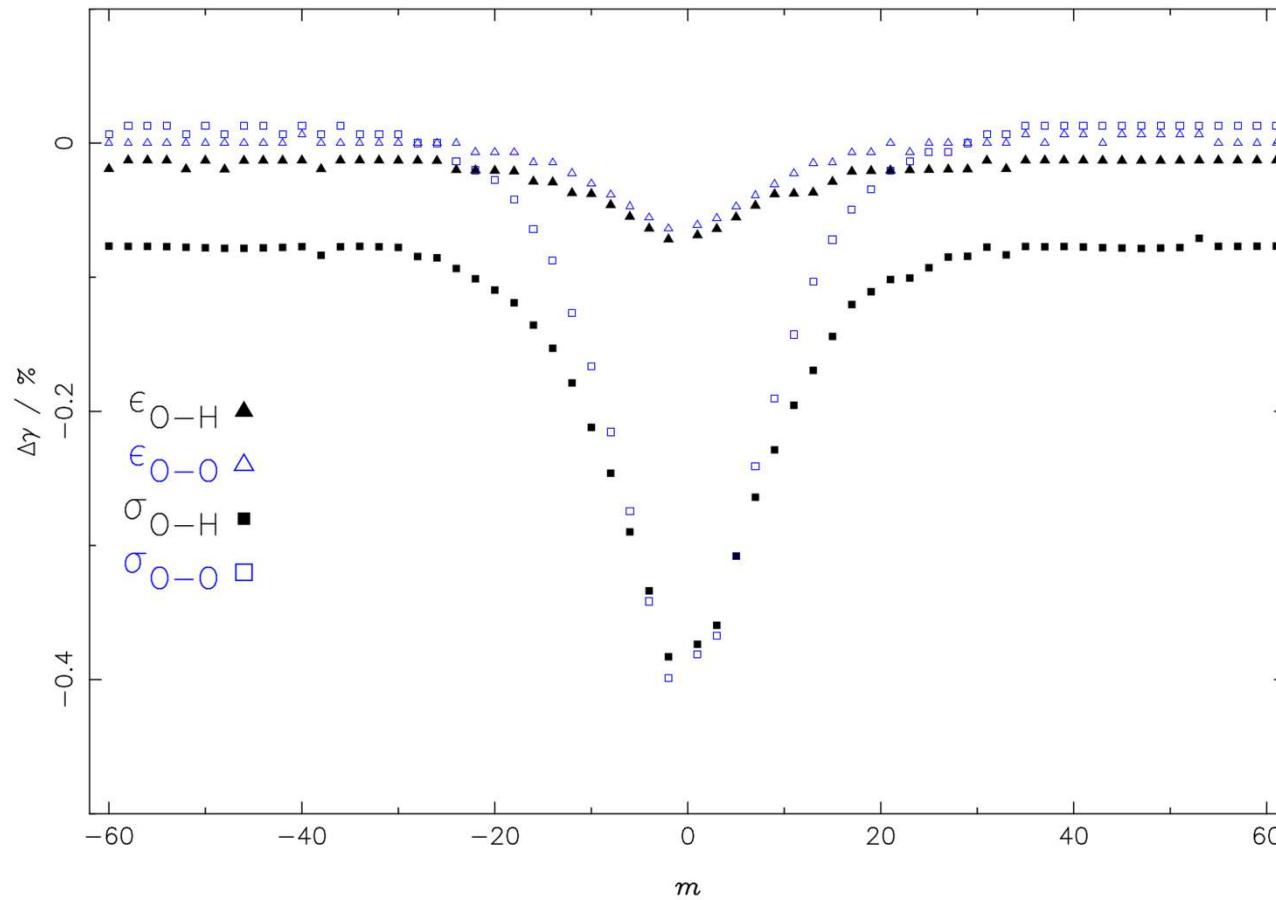


APD: 0.57% (SD: 6.16%)

Renaud et al., Icarus (2018), 306, 275

Line shape calculations

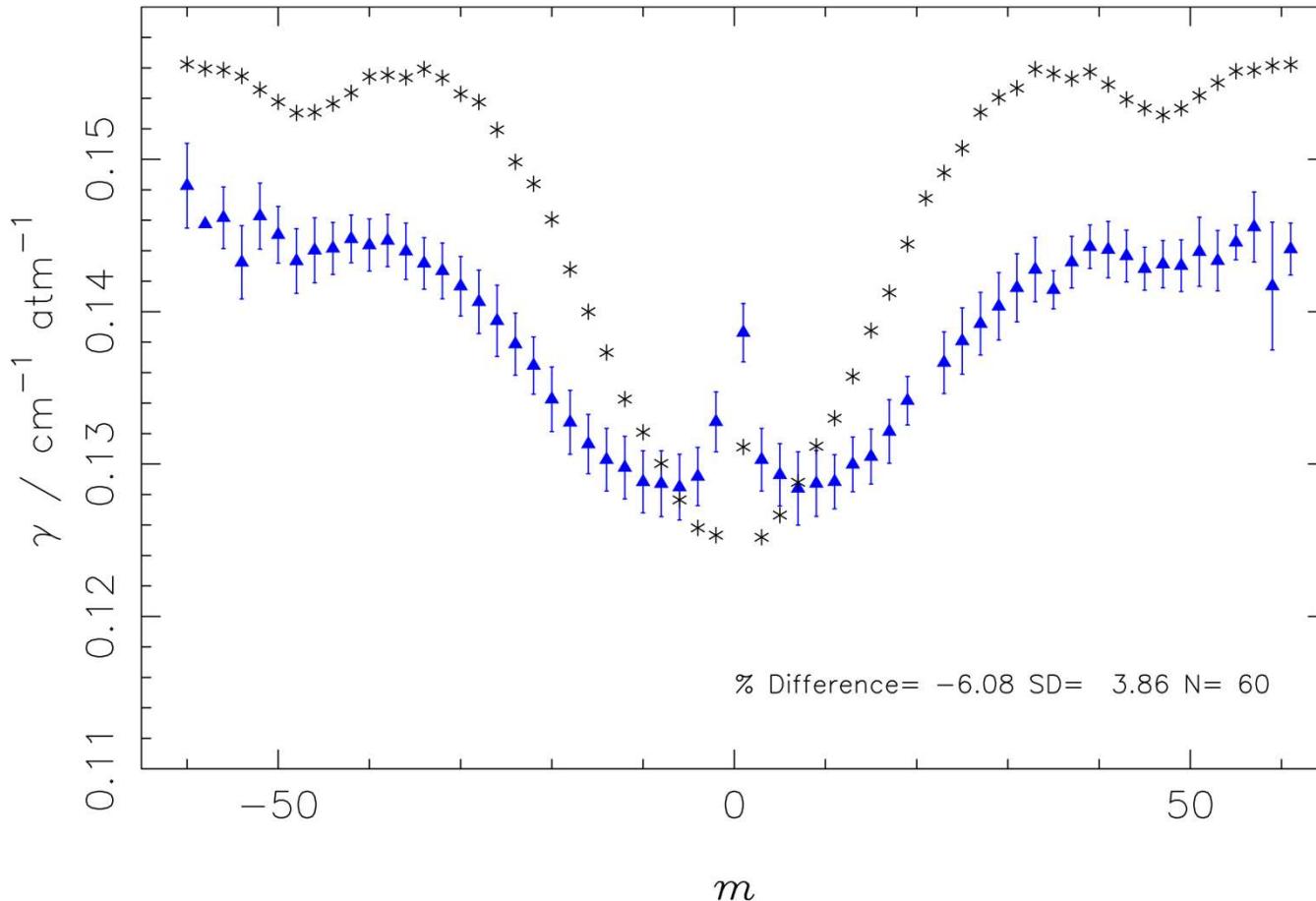
Potential determination ($\text{CO}_2\text{-H}_2\text{O}$)



Vispoel & Gamache, JQSRT, 316, 108896 (2024)

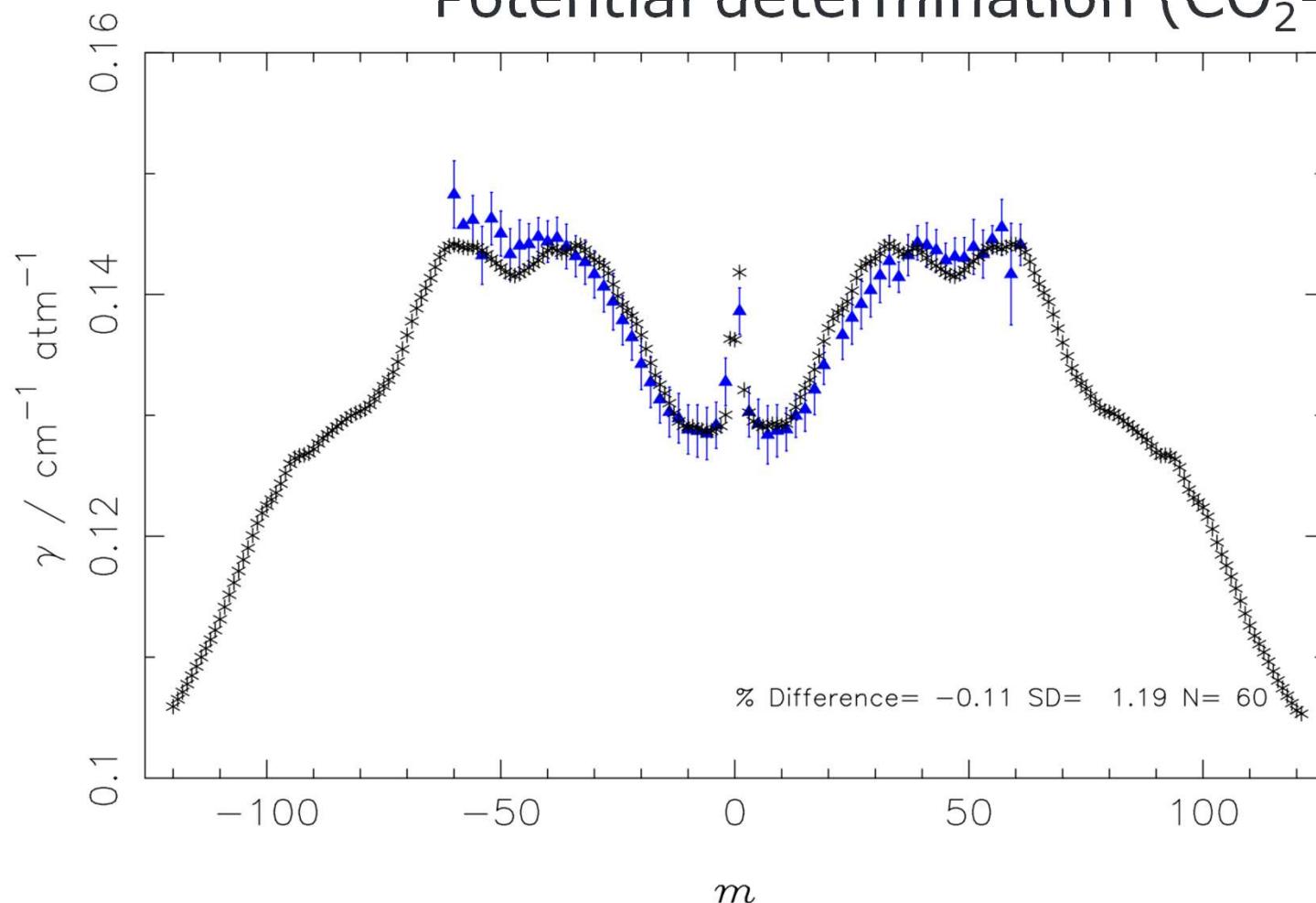
Line shape calculations

Potential determination ($\text{CO}_2\text{-H}_2\text{O}$)



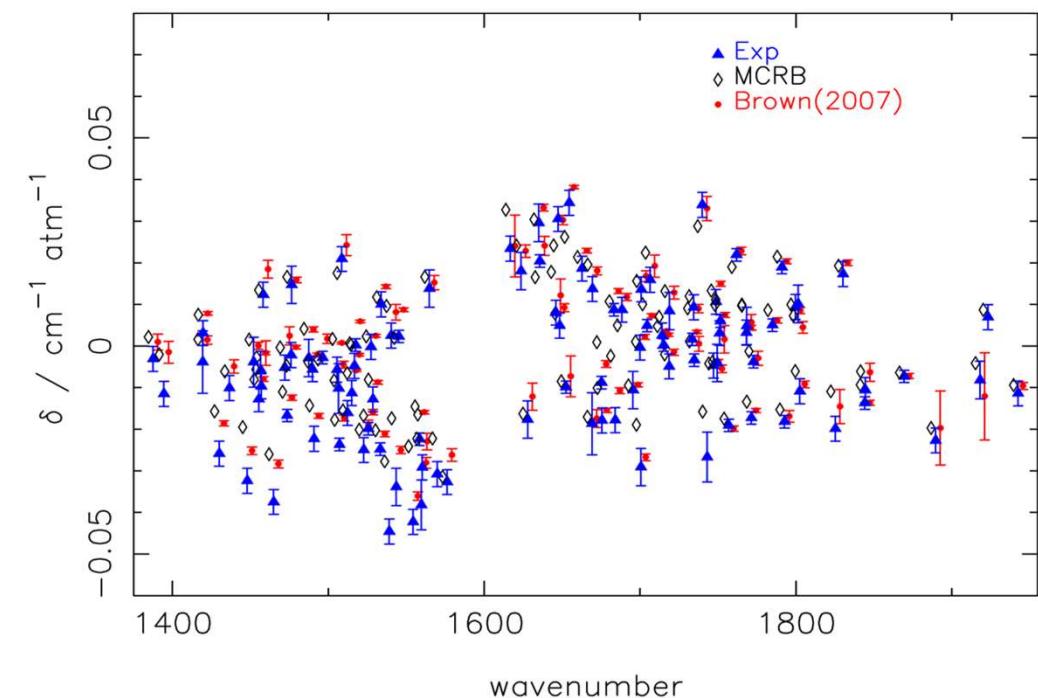
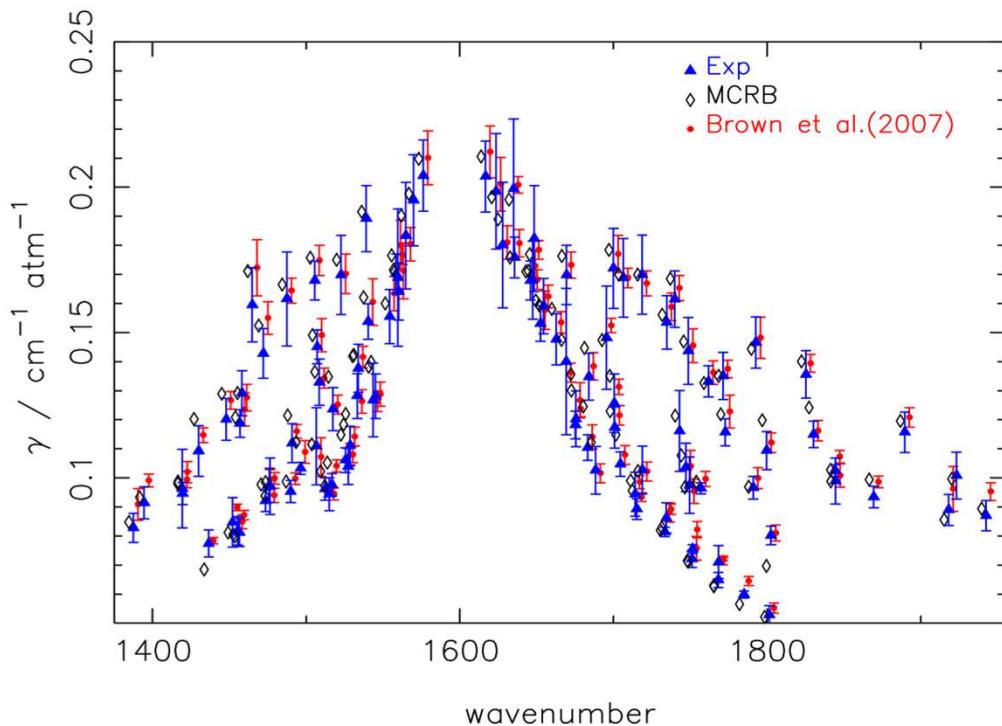
Line shape calculations

Potential determination ($\text{CO}_2\text{-H}_2\text{O}$)



Line shape calculations

Potential determination



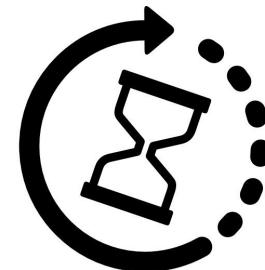
Régalia et al., JQSRT, 231, 126 (2019)

Line shape calculations

What next ?

HITRAN 2020 (H_2O)

- 319 887 transitions
- 555 different vibrational bands



- Make calculations for selected bands
- Develop a physic's-based prediction algorithm

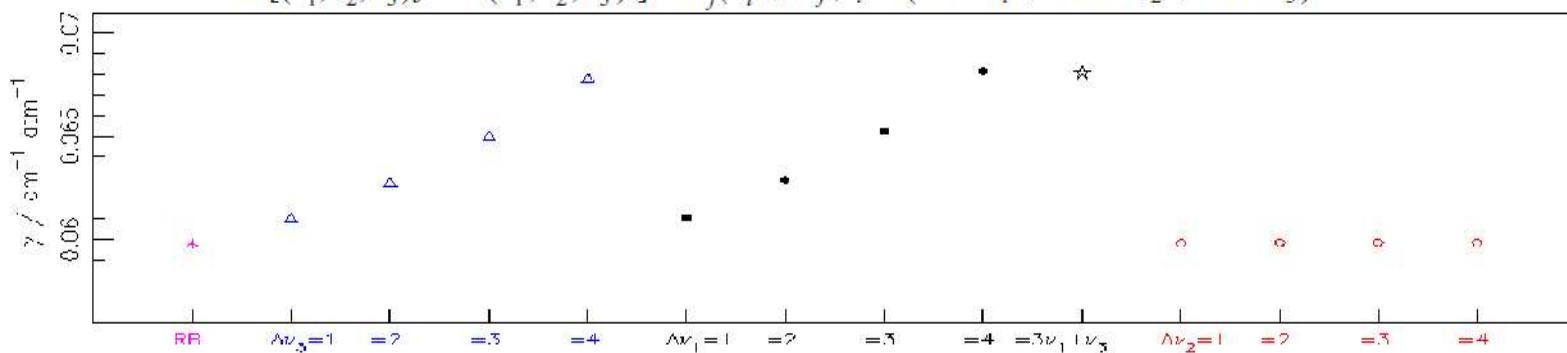
Line shape calculations

Vibrational dependence – Prediction routine

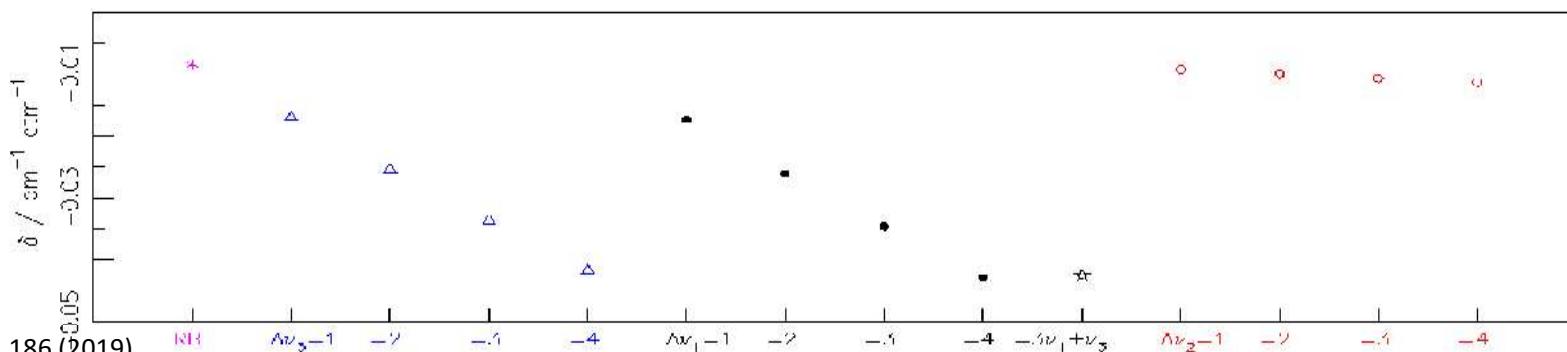
$$\gamma[(v'_1, v'_2, v'_3) f \leftarrow (v''_1, v''_2, v''_3) i] = \gamma_{f \leftarrow i}^0 + A_{f \leftarrow i} \times (0.3\Delta v_1 + 0.07\Delta v_2 + 0.3\Delta v_3)^2,$$

$$\delta[(v'_1, v'_2, v'_3) f \leftarrow (v''_1, v''_2, v''_3) i] = \delta_{f \leftarrow i}^0 + B_{f \leftarrow i} \times (0.3\Delta v_1 + 0.07\Delta v_2 + 0.3\Delta v_3).$$

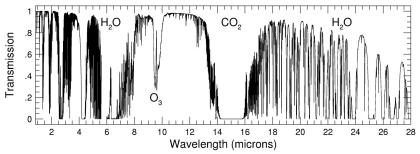
$\text{H}_2\text{O}-\text{H}_2$



H₂O–H₂ vibrational dependence 9 o 9 ←← 10 + o

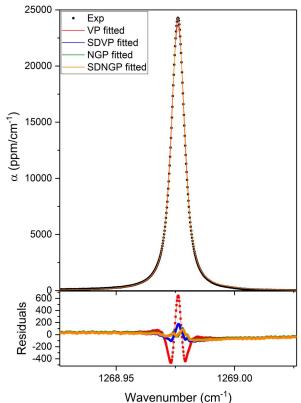
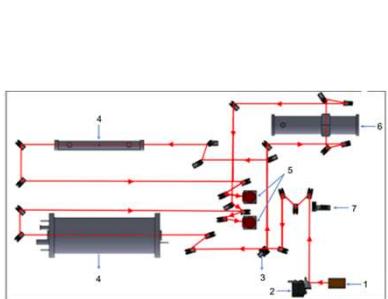


Summary

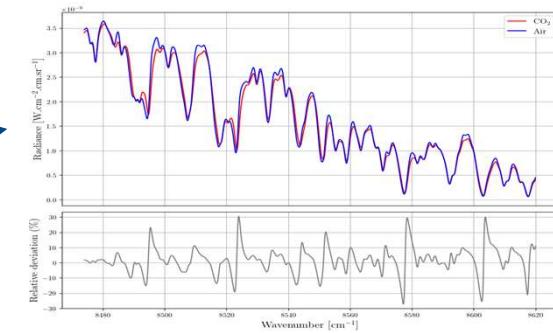


Spectroscopic parameters

Experimental measurements



Improve radiative transfer



Line shape calculations

$$(\gamma - i\delta)_{f \leftarrow i} = \frac{n_2}{2\pi c} \int_0^{+\infty} v f(v) dv \int_0^{+\infty} 2\pi b db \times \left[1 - e^{-i\langle S_1 + \text{Im}\{S_2\} \rangle_{J_2}} e^{\langle \text{Re}\{S_2\} \rangle_{J_2}} \right]$$

- CRBM calculations
- Prediction routine

WHO is WHO?



Dr Laurence Régalia
Maitre de conférences



Dr Séverine Robert
Head of "Planetary Atmospheres"
research unit



Prof. Robert R. Gamache
Professor Emeritus

Thank you for your attention